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Energy Bond Graphs

a semiotic formalization of modern physics

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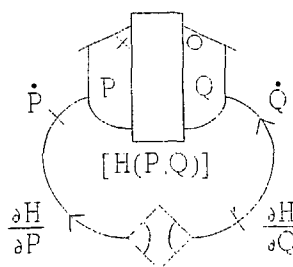
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Energy Bond Graphs— —a semiotic formaliza- tion of modern physics



Peder Voetmann Christiansen

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Energy Bond Graphs - A Semiotic Formalization of Modern Physics

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Abstract

This paper gives a brief introduction to the Energy Bond Graph (EBG) formalism - A modelling technique originally intended for Engineering and Ecological Energetics. The formalism is a shape-value notation built on C. S. Peirce's phenomenology and semiotics. Besides being a didactical tool for teaching physics to experienced students the formalism has proved valuable in connection with both the experimental and the theoretical physics research conducted at IMFUFA during the last 25 years.

The front page illustration shows the EBG formulation of Hamilton's equations.

Energy-bond-graphs — a semiotic formalization of modern physics.

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1. Scope of the formalism

An Energy Bond Graph (EBG) is a comprehensive diagrammatic representation of all the relations that constitute a dynamical system. As such, it is a mathematical model, but not just mathematical. The EBG formalism requires a total reduction to physical standard relations that exist both as hardware and as software. It thus resembles a program or a wiring diagram for an analog computer representing both a set of equations and a construction-recipe for a real system that acts out the equations. EBG modelling is a "glass-bead-game" — a "fundamentalist" way of doing physics (proceeding from real fundamentals), like Peirce's Existential Graphs are to logic. Peirce said in his second Lowell Lecture from 1903 that he had spent forty years of his life developing the existential graphs and he described its purpose in the following way that may just as well serve as an introduction to the EBG-formalism:

"Before beginning, let us distinctly recognize the purpose which this system of expression is designed to fulfil. It is intended to enable us to separate reasoning into its smallest steps so that each one may be examined by itself. Observe, then, that it is *not* the purpose of this system of expression to facilitate reasoning and to enable one to reach his conclusion in the speediest manner. Were that our object, we should seek a system of expression which should reduce many steps to one; while our object is to subdivide one step into as many as possible. Our system is intended to facilitate the *study* of reasoning but not to facilitate reasoning itself. Its character is quite contrary to that purpose."

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The EBG-technique is not an easy way to mathematical models in physics, because it forces the user through an initial phase of semiotic reflections on categorization of variables, etc. This initial work, however, will lead to insights that are not easily gathered from more direct modelling techniques.

2. Classification of dynamic variables.

There are four kinds of dynamic variables in the EBG-formalism, and these are conveniently displayed in a Greimasian semiotic square. This method needs two pairs of binary opposites. The two members of a pair of opposites are placed diagonally against each other in the corners of a square, and then the four sides of the square identify the possibilities.

The two pairs of opposites are:

- 1: Level/rate, where the level-variables are accumulated, i.e. they can only change by time-integration of associated rates, whereas the rates may change abruptly.
- 2: directed (x)/undirected (o). Directed variables have direction both in space and time, i.e. they require a spatial orientation-convention and they change sign by time-reversal. Thus, we get the semiotic square of figure 1:

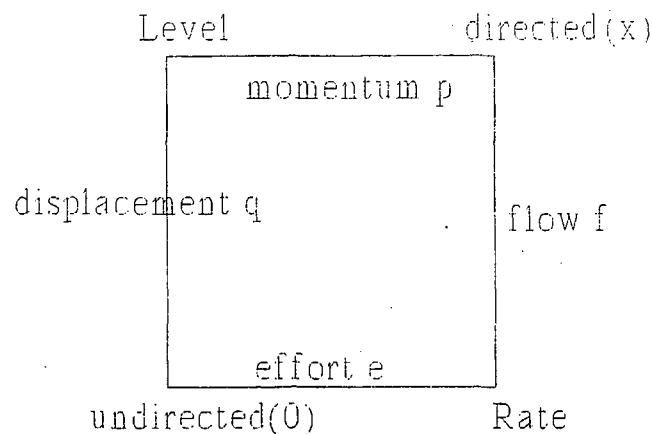


figure 1 Semiotic square of dynamic variables.

In EBG diagrams the levels are associated with "bird-house" storage icons (inspired by H.T. Odum)¹ marked x for kinetic energy and o for potential energy, while the rates are marked on the line-icon of an energy-bond with an arrow for the directed flow and a stroke for the undirected effort. The consideration that efforts (forces) are undirected reflects a deep law of classical mechanics, namely Newton's law of action and reaction.

Figure 2 below shows how the same system — a harmonic oscillator — is depicted by the present author (a) and with the more austere drawing style of the EBG-formalism's inventor H.M. Paynter (b).²

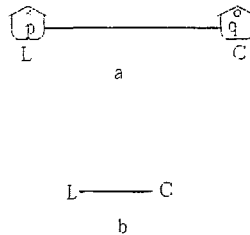


figure 2 Harmonic oscillator

3. Shape-value-notations

The difference between the two diagrams in figure 2 illustrates the concept of a *shape-value notation* (a) where the shape of the icons is chosen such as to convey an idea of their value or function and a *symbolic notation* where symbols like digits or letters are used to replace proper icons (b).

The present formulation was inspired by Odum's shape-value-notation for Ecological Energetics¹, but it was felt that the lack of physical precision in Odum's definitions of his icons could be remedied by using Paynter's bond-graphs². However, Paynter did not attempt to create suitable shapes for his icons and reverted to a symbolic notation, which lead to some ambiguities. By using, e.g., the letter T as an icon for a transformer/transducer one misses the fact that a proper definition of the

parameter of the object requires a distinction between its *primary* and its *secondary* port, and this distinction cannot be brought out by a symmetric shape like T, but only by an asymmetric icon (except in special cases), like the triangular shape in figure 6.

Some icons have associated parameters, denoted by symbols. The shape-value notation demands that the meaning of these symbols shall be uniquely defined by the shape of the icon. This demand means that it is sometimes necessary to have two different icons for the same physical function, as with the gyrators and the sinks shown in figure 6.

Attempts to create shape-value-notations for mathematics and logic have been studiously ignored by mathematicians, who for the last hundred years have preferred to continue in the trend laid out by Hilbert's shapeless axiomatization of Geometry. Thus was neglected Peirce's construction of a shape-value-notation for the sixteen binary logical connectives³ Peirce's notation was rediscovered by Shea Zellweger who has now developed it further to a complete "logic alphabet" thereby stressing the merits of shape-value notations for educational purposes⁴ Peirce's early version of his existential graphs (the alpha graphs) was also a shape-value notation of logic and a precursor of Spencer-Brown's "Laws of Form" from 1969.⁵

By developing the EBG-formalism as a shape-value notation the present author hopes to have helped strengthening an important historical strain that may prove valuable to Physics and Biosemiotics.

4. Basic response properties.

In a response experiment we act on a system through an energy bond, which, as we have seen, contain four variables, q, f, e , and p . These four variables are not independent, because the levels q and p are time-integrals of the rates f and e . In the experiment we leave the system undisturbed from time $-\infty$ to time 0. Then we choose one of the four variables as *stimulus* s and let it have a constant value from time 0 to ∞ . As there are two causal groups of independent variables we can choose s from one group (e.g. (f, q)) and then observe the response $r(t)$ as one of the variables from the other group (e, p). In the response-matrix shown in figure 2 there are thus two windows of possible response-properties, each containing four functions, but it can be shown that for *time-homogeneous*

systems where the result does not depend on which instant we choose as time 0, two of the four functions in each window will be identical. Any physical system therefore has six different response-properties.

	s				
r	q	f	e	p	
q			J	Y	
f			Y	F	
e	G	Z			
p	Z	M			

figure 3. the matrix of response-functions.

Response-semantics, i.e. the choice of proper nouns to denote the response-properties may then proceed from the *response-semiotics* of figure 3. In the following table we have combined usually used nouns with the six two-link Peircean sign classes: Read, e.g. (23) as "second of third".

- (11) G: *Rigidity* or *elastic modulus*.
- (12) Z: *Impedance* or *resistance*,
- (22) M: *Inertance* or *Inductance*.
- (13) F: *Lightness* or *Susceptibility*.
- (23) Y: *Conductance* or *Mobility*.
- (33) J: *Compliance* or *Capacitance*.

We have here defined the response-functions as functions of time from 0 to ∞ , but by Laplace-Stieltjes-transformations they are defined as functions of a complex frequency $s = -i\omega$. These complex functions are usually just called *generalized susceptibilities*.

However, there are many advantages in distinguishing the different functions by different names because they are mathematically related by time-integration: G integrates to Z, Z integrates to M, and similarly for the set F,Y,J. In the frequency- (s-) domain time integration corresponds to division by s. Thus, by this semiotic/semantic approach it becomes

possible to identify and name a response-property after a quick glance at the oscilloscope. And a careful distinguishing by names serves to develop the somewhat mysterious ability called "physical intuition".

5. the energy bond, causality and orientation.

the most basic icon of the EBG-formalism — *the energy bond* — is drawn as a simple line. It denotes an energetic *interaction* between two system-components. The interaction is mediated by the two rate-variables that belong to the bond: the directed *flow*, f , indexed as an arrow and the undirected *effort*, e , indexed as a stroke. If system A acts on system B with an effort, then system B acts back on system A with a flow. This causality is then indicated by placing the effort-index closest to B and the flow-index closest to A. By using an arrow as the flow-index we are forced to choose an *orientation* of the bond. Every bond may have either orientation, but when we want to view the same physical situation with the opposite orientation, we have to change the sign of the symbolic expression for the flow (f changes to $-f$). The interaction between A and B described above can thus be depicted in the two ways shown in figure 4:

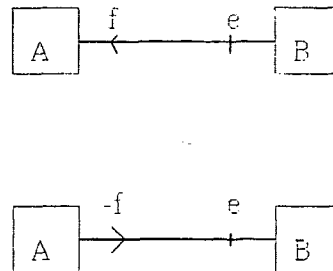


Figure 4 Interaction and orientation.

It must be stressed that the causality of an energy bond is not just a formal consideration made necessary by the algorithmic ordering. There

exists a precise measurement prescription to decide the causal order of the rate-variables for each bond, based on the analysis of transients or noise.

Every energetic interaction is associated with a flow of energy. The energy flow in the direction of the orientation of the bond is the product of effort and flow.

In general effort and flow are defined as *vectors in a complex metric space of arbitrary dimensionality*. The energy flow is then defined as the *scalar* product of the effort- and the flow-vector. This generalization, however leads to the complication that the vectors must be represented as either *covariant* or *contravariant*. The flow-orientation rule shown in figure 4 then has to be modified such that the change of orientation is associated with a shift of variance of both the effort- and the flow-vector. By adopting the further rule that *the same physical situation may be described with either variance of the effort* (but not of the flow), the formalism becomes able to treat vectors of mixed kinds where some of the effort-components are flows and the corresponding flow-components are efforts. This feature allows for a very general treatment of response-experiments, where, e.g. the celebrated *Onsager symmetry relations* becomes a theorem of the EBG-formalism.

The general vector-formulation also demands that *each bond is associated with a metric tensor* that relates the covariant to the contravariant vectors. A unit metrical tensor is represented as a matrix with 1s in the diagonal and 0s outside. This is *Euclidean metric*. When coordinate vectors are defined by three spatial coordinates and one time-coordinate the flow-vector's first three components will be flows and the fourth will be an effort. This corresponds to a metric tensor with 1s in the three first places of the diagonal and -1 in the fourth place — *the Minkowsky-metric*. The group of metric-preserving transformations for this metric are *the Lorentz-transformations*, and the whole formalism of special relativity follows from this. Likewise, by adopting the general tensor-formulation of *Riemannian metric spaces* the theory of general relativity also follows from the EBG-formalism.

6. Definitions of basic icons

EBG-modelling always proceeds through three semiotic stages: from *icons* through *indices* to *symbols*. Each icon denotes a basic physical relation between the input and output variables of the associated bonds (the *ports*). When indices — flow-arrows and effort-strokes are marked on the bonds, symbolic expressions for these variables are written near the indices, whereby the meaning of the symbols and the function of the icon is defined. Note that *nearness* is itself an indexical element inherent in the meaning of the symbols. Symbols near the icons are also used for defining certain parameters of the icons (like storage-capacity and transformer-ratio).

The basic icons are clearly divided in three classes corresponding to Peirce's three phenomenological categories:

- 1: *Active* systems (sources of flow or effort) have an output-variable that is independent of the input-variable.
- 2: *Passive* or *reactive* systems have an output that is determined by the present or the previous values of the input.
- 3: *Dissipative* systems (the sinks) mediate between active and passive behaviour. Their response is mainly passive, like the voltage over a resistor, given by Ohm's law, but the passive response is superposed with an active component — the *noise* — that depends both on the sink-parameter and the temperature.

In figure 5 we show definitions of the active and the reactive systems.

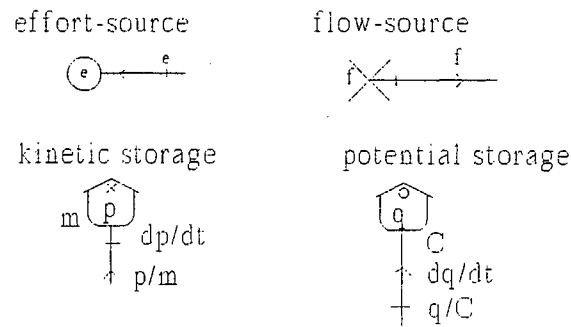


figure 5 active (sources) and reactive systems (storage)

Figure 6 shows the sinks and two passive 2-ports, transducer/transformer and gyrator. The definition does not distinguish between transducer and transformer, but the name "transducer" is used when the parameter t has a physical dimension, whereas transformers are dimensionless. Transformers and gyrators are very different although they look similar. The parameters t and g may be given as level-variables elsewhere in the system, but then t must be an undirected level, whereas g must be directed. Such *parametric feedback* is useful for modelling nonlinearities.

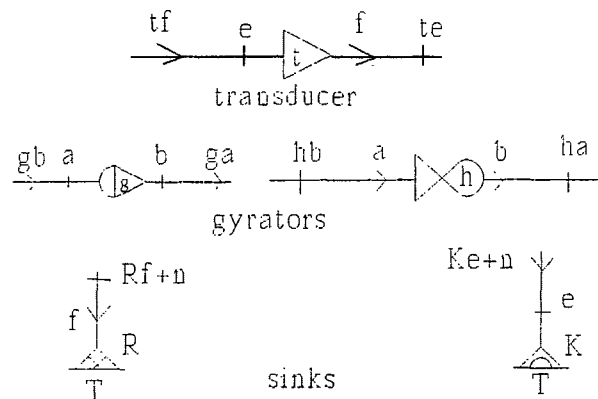


figure 6 Passive 2-ports and sinks (n denotes noise).

Finally, figure 7 shows the *junctions* as 3-ports, thus representing the only *triadic* relations of the formalism. The junctions are *topological* constraints corresponding to Kirchhoff's two laws of electrical networks. The o-junction corresponds to a node in the network (parallel connection) and the x-junction to a mesh (series connection). The similarities between o- and x-junction reflect the nearly dual symmetry between efforts and flows, but the dual symmetry is broken by the fact that flows are directed, while efforts are not, and this leads to subtle differences between the junctions, which, however, we shall not discuss here.

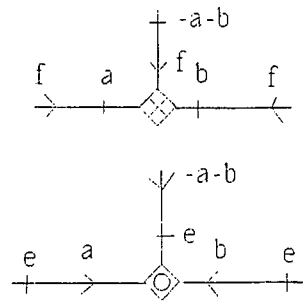


figure 7 The junctions.

7. Beyond laws of nature

A strange consequence of the EBG-game is that what we usually regard as laws of nature seem to vanish out of scope. Instead we have the rules of the game, which ensure that the laws of nature are obeyed. The vanishing of laws is thus a result of mathematization and semiotization. Similarly, in elementary physics the pupils learn the law of nature that forces are combined by the construction known as the parallelogram of forces, but in more advanced teaching they are just taught that forces are *vectors*, so the former law of nature becomes the rule for adding vectors.

We have seen that Newton's law of action and reaction hides within the rule that efforts are undirected or the flow-orientation rule of figure 4. Similarly, we can find Newton's second law of motion (force equals mass times acceleration) in the definition of the x-storage icon of figure 5, where m is the mass, p the momentum, e the force, and f the velocity (p/m). It was also mentioned that Onsager's symmetry- or reciprocity-relations is a theorem of the EBG-formalism. It is therefore not necessary for users of the formalism to know this as a law of nature, because it is automatically satisfied by all EBG-models that are made according to the rules.

Certain combinations of icons are not allowed, because they lead to *causal conflicts*. It is absolutely forbidden to connect two effort-sources directly or through a transformer. The sources are absolutely rigid in their causality, while other systems may be forced to yield. By connecting an effort source to a o-storage a mild conflict arises where the storage element is forced to give in and accept "differential causality". In this

way we are allowed to ascribe a conductivity to an electric, capacitor C , but the conflict still shows itself in the fact that the frequency-dependent conductivity C_s goes to infinity for large frequencies, which means that the causality will break down if the effort of the source changes very rapidly. Causal conflicts may often be resolved by introducing extra sinks. This happens, e.g. when a car tries to accelerate too fast; the wheels will slide on the road — a sink has appeared to represent the friction between wheel and road. In the traditional way of describing physical systems — by equations — there is no formal treatment of causality, so the concept of causal conflict does not exist, but in reality it plays an important role, especially when systems break down.

Many laws of nature are formulated as partial differential equations, e.g. the diffusion- and wave-equations, Maxwell's electromagnetic equations, and the Schrödinger equation. Such equations are in EBG diagrams shown by combining icons, each representing an infinitesimal section of space in structures that are repeated in three dimensional space like the atoms in a crystal. As an example of this figure 8 shows the unit cell for representing Maxwell's equations in vacuum. Not shown in the diagram are storage elements connected to the junctions: x-storage to x-junctions representing the magnetic induction-vector \underline{B} , and o-storage to o-junctions representing the electric displacement-vector \underline{D} . The electric field \underline{E} and the magnetic field \underline{H} are represented, respectively, as the efforts and the flows in the bonds.

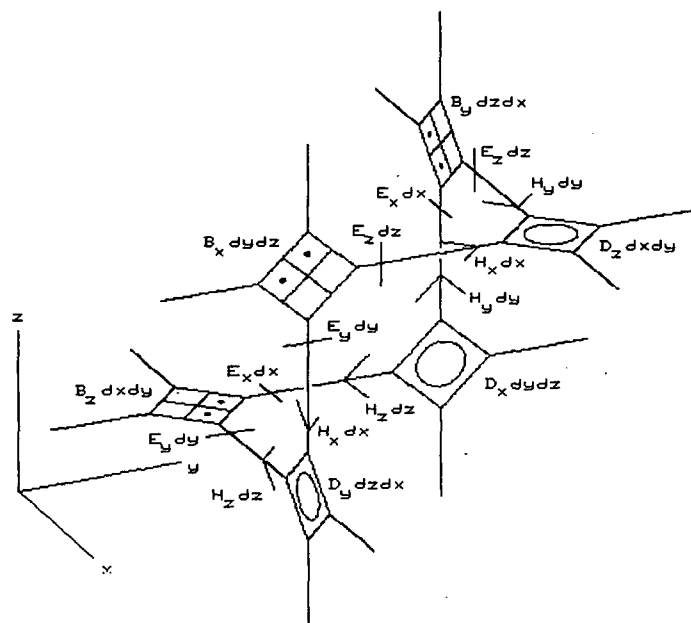
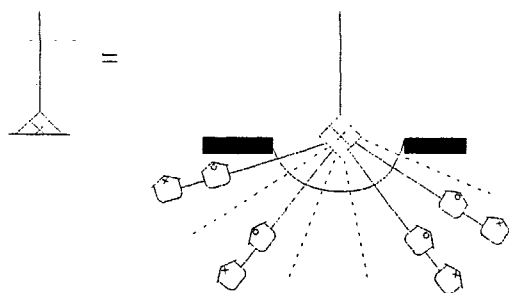


Figure 8 Unit cell for Maxwell's equations.

As mentioned, the sinks are sources of noise. This important insight follows from the *Fluctuation-Dissipation Theorem* by Callen and Welton (1951)⁶. As shown in figure 9 and the associated formula the complete complex impedance function $Z(\omega)$, ($\omega = i s$) may be spectrally resolved on the response-functions of harmonic oscillators. The real, or dissipative part of the impedance $R(\omega')$ is proportional to the density of oscillators on the real axis of their resonance frequencies ω' . The spectral resolution formula is then valid when ω has a positive imaginary part. This formula is translated to icons in the figure and gives justification for the choice of the sink-icon. The noise is simply the output from all these uncorrelated oscillators in thermal equilibrium with the temperature T . For an ohmic resistance the oscillator-frequencies will be equally distributed over the real axis, and the noise-spectrum will be *white*.



$$Z(\omega) = \frac{i}{\pi} \int_0^{\infty} R(\omega') \left[\frac{1}{\omega - \omega'} + \frac{1}{\omega + \omega'} \right] d\omega'$$

figure 9 Spectral resolution of a sink

For a frequency-independent resistance R the prescription of the FD-theorem is simply that for each step dt of the numerical integration one has to add the effort-noise

$$n = N(\sqrt{(2RkT/dt)})$$

to the passive response of the sink. Here $N(x)$ is a normally distributed random number with mean value 0 and standard deviation x . k is Boltzmann's constant, and T the absolute temperature. The formula is valid in the *classical limit*, when $dt \gg \hbar/kT$.

It is noteworthy that the noise diverges to infinity when the steplength dt goes to zero. The noise is, as Peirce said,

"infinite in the here-and-nowness of immediate sensation, finite and relative in the recency of the past". (CP 6.135).

Every EBG-model containing dissipative elements thus becomes "animated with noise". It is easy to show that the level-variables of the system in this way get the exact fluctuation-moments that are prescribed by Statistical Mechanics, which in this way also becomes a result of the EBG-formalism.

The above expression for the effort-noise n demands that the sink-parameter R be positive. This is a further axiom of the formalism and it has the result that the energy flow to a sink, $R\dot{f}^2$ is always positive, thus ensuring that the laws of thermodynamics are always obeyed by EBG-models.

8. Completeness of the formalism

Within *Physics* and *Engineering* the EBG-formalism seems to be complete. Although new icons can be freely invented and added to the basic icons it seems always possible to make a full *reticulation*, i.e. to reduce these new functions to the basic icons. In practice it is easier to use a combination of basic and composite icons. The icons used by the author, shown in figure 10, are defined once and for all in an object-oriented drawing program (DrawPerfect 1.1)

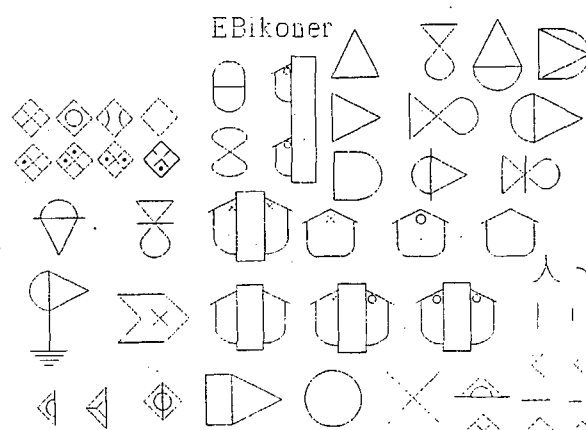


figure 10 Iconic objects of the EBG-formalism

A full proof of completeness is difficult to find (if not impossible), but many special cases have been considered⁷ and algorithmic prescriptions for their translation to the EBG language have been found, of which I shall just mention a few:

1 *Chemical reactions* forwards and backwards were first described by a reaction-icon based on H.T. Odum's *work-gate-icon*, but it was later shown that the reaction-icon can be reticulated by sinks and gyrators. In this way it is possible to make EBG-descriptions of large biochemical reaction-networks, like photosynthesis.

2 Topology of electrical and rheological networks are easily translated to EBG diagrams of junctions. It turns out, however, that the x-junction is a series connection in electricity but a parallel connection in rheology (and vice versa for the o-junction).

3 Linear response can be reduced to electrical networks⁸, and from there to EBG models. So in this case a full proof of completeness exists. On the other hand it is not always possible to translate EBG diagrams to electrical networks. (It may lead to short-circuits if one tries).

4 All systems that can be described with the Lagrangian and Hamiltonian methods of classical analytical mechanics can be translated to EBG-models by a relatively simple algorithm. So in this case the formalism is also proven complete, and it turns out that the EBG-models are generally more efficient for simulation than the Hamiltonian equations.

5 All relations exhibited by the basic icons are linear, but, as mentioned earlier, non-linearities may be introduced by parametric feedback from levels to transformers and gyrators. Such non-linearities will contain a time-delay, but many systems of classical mechanics require *simultaneous* non-linear relations. Such relations can also be given by an EBG diagram. In figure 11 it is shown how a simultaneous rendering of the relations $s=\sin\theta$ and $c=\cos\theta$ is reticulated:

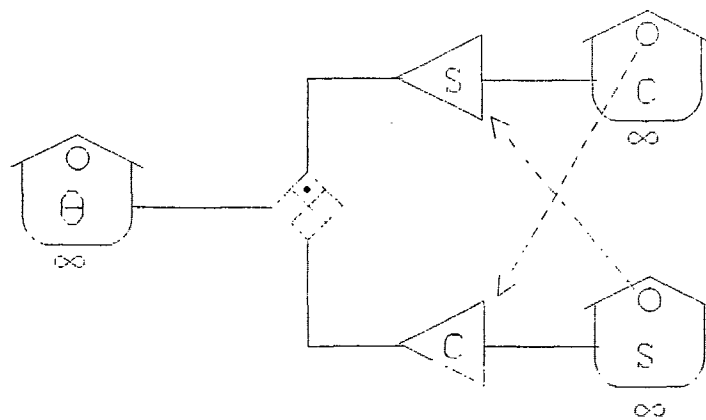


figure 11 Simultaneous reticulation of $c=\cos\theta$ and $s=\sin\theta$.

Finally, figure 12 shows how a complicated mechanical system — a double-pendulum — is fully reticulated with all its cosines and square-roots:

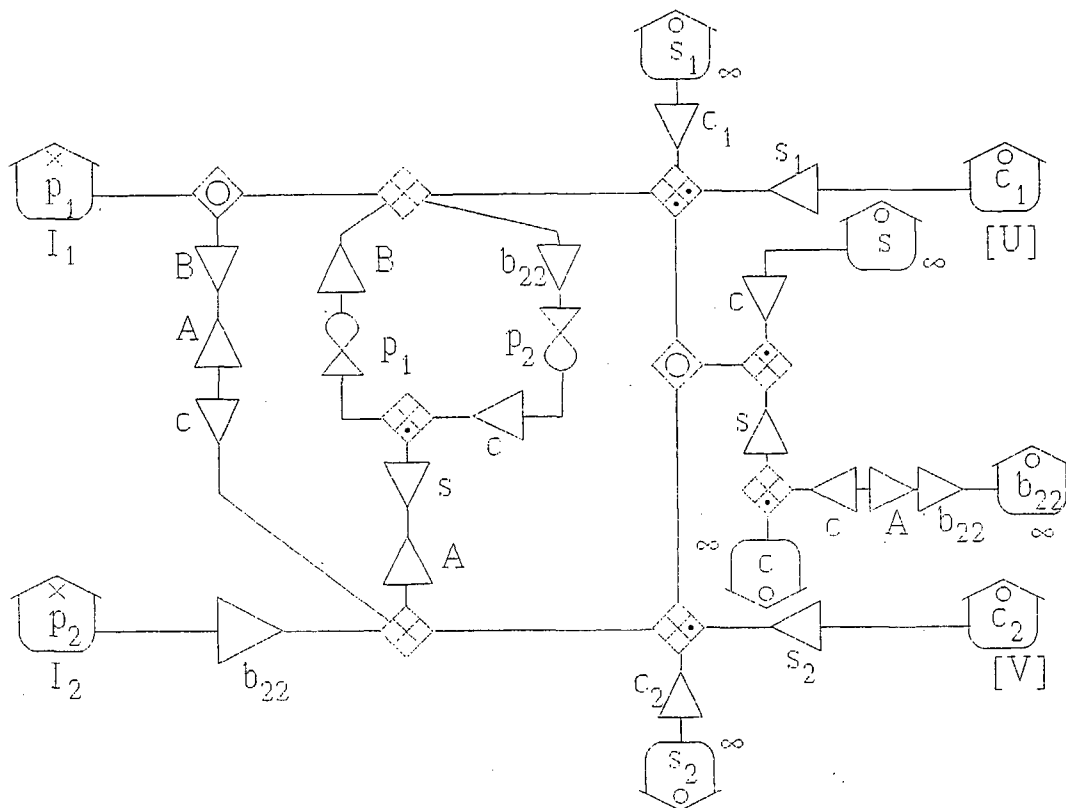


Figure 12 Full reticulation of double-pendulum.

9. Perspectives

Some biosemioticians are apprehensive about the dangers of physical reductionism. It must be admitted that EBG-formalism is an example of such reductionism, and even that it tries to carry physical reductionism to an extreme (by reducing basic physical concepts to even more basic semiotic concepts). Against such warnings I have several comments:

- 1): Kurt Gödel carried logical positivism to an extreme and found something on the other side of great importance to mathematics and philosophy.
- 2) An EBG-model is always open to expansion into the environment, except when the underlying theory demands a closure.
- 3) Regarding Biosemiotics: An EBG model is a sign of a general idea and thus, as Peirce said (CP 6.270) a living entity analogous to a person. The variables in an EBG-model are always superposed, both with thermal noise and quantum-fluctuations, that may be regarded as "living feeling" and spontaneity. If it is reductionistic to use such models in biology, it is, at least, not a simplistic kind of reductionism.
- 4) Regarding Quantum Mechanics: The EBG-formalism has a strong affinity to Quantum Mechanics, as it has to Relativity. If it becomes possible to construct an analog computer that can act out all the simultaneous feedbacks of EBG-models, it will be a quantum computer. The non-local constraints exhibited by the junctions give a simple explanation of Quantum-Non-Locality (the Einstein- Podolsky-Rosen experiments). Many other seemingly counter-intuitive quantum mechanical effects also appear as natural and understandable when viewed in the light of EBG-

reticulation of the physical sign-relations. A full investigation of this research program, called *Quantum Semiotic*, is in progress, but may take many years to complete.

Lejre, july 1. 2003

Peder Voetmann Christiansen.

10 References

1. H.T. Odum *Environment, Power, and Society*, Wiley, N.Y. 1972.
2. H.M. Paynter, *Analysis and Design of Engineering Systems*, M.I.T. Class notes, 1961.

D. Karnopp and R.C. Rosenberg, *Analysis and Simulation of Multiport Systems — The Bond Graph Approach to Physical System Dynamics*. The M.I.T. Press, Cambridge, Mass., 1968.
3. Louis H. Kauffman *The Mathematics of Charles Sanders Peirce*, Cybernetics and Human Knowing, vol. 8, No. 1-2, 2001
4. Shea Zellweger: *Mathelological Semiotics: A Lesson in constructing a Shape-Value Notation for Elementary Logic*. In: Myrdene Anderson et al. (ed.s) *Educational Perspectives on Mathematics As Semiosis: From Thinking To Interpreting To Knowing* Legas Publishing, Toronto, 2003.
5. G. Spencer-Brown: *Laws of Form*, George Allen & Unwin, Ltd. London 1969.
(See also the article by Jack Engstrom in ref. 3).
6. H.B. Callen and T.A. Welton. *Phys. Rev.* **83**, p. 208, (1951).
7. Peder Voetmann Christiansen *texts about the EBG-Formalism*, Tekster fra IMFUFA, Roskilde Universitetscenter (all in danish) The series includes texts no. 8 (1978), 22 (1979), 238 (1993), and 296 (1995). No. 22 discusses linear response and noise, no. 238 the vector and tensor formulation including relativity theory, and no. 296 Classical Analytical Mechanics.
8. M.E. van Valkenburg, *Introduction to Modern Network Synthesis*, Wiley, 1960.

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- 338/97 Kvantisering af nanolederes elektriske ledningsevne
 Første modul fysikprojekt
 af: Søren Dam, Esben Danielsen, Martin Niss,
 Esben Friis Pedersen, Frederik Resen Steenstrup
 Vejleder: Tage Christensen
- 339/97 Defining Discipline
 by: Wolfgang Coy
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 by: Carsten Lunde Petersen
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 by: Mogens Niss
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 for the project LONG-TERM SCENARIOS FOR GLOBAL ENERGY DEMAND
 AND SUPPLY
- 343/97 IMPORT/EKSPORT-POLITIK SOM REDSKAB TIL OPTIMERET UDNYTTELSE
 AF EL PRODUCERET PÅ VE-ANLÆG
 af: Peter Meibom, Torben Svendsen, Bent Sørensen

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 by: Carsten Lunde-Petersen
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 Ph.D. Thesis
 by: Mette Sofie Olufsen
- 346/98 Klyngedannelse i en hukatode-forstøvningsproces
 af: Sebastian Horst
 Vejledere: Jørn Borggren, NBI, Niels Boye Olsen
- 347/98 Verificering af Matematiske Modeller
 - en analyse af Den Danske Eulerske Model
 af: Jonas Blomqvist, Tom Pedersen, Karen Timmermann, Lisbet Øhlenschläger
 Vejleder: Bernhard Booss-Bavnbek
- 348/98 Case study of the environmental permission procedure and the environmental impact
 assessment for power plants in Denmark
 by: Stefan Krüger Nielsen
 project leader: Bent Sørensen
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 arbejdsmarkeduddannelserne
 af: Lena Lindenskov og Tine Wedege
- 350/98 OPGA VESAMLING - Bredde-Kursus i Fysik 1976 - 1998
 Erstatte teksterne 3/78, 26/93 og 322/96
- 351/98 Aspects of the Nature and State of Research in Mathematics Education
 by: Mogens Niss
- 352/98 The Herman-Swiatec Theorem with applications
 by: Carsten Lunde Petersen
- 353/98 Problemløsning og modellering i en almindelig matematikundervisning
 Specialrapport af: Per Gregersen og Tomas Højgaard Jensen
- 354/98 A Global Renewable Energy Scenario
 by: Bent Sørensen and Peter Meibom
- 355/98 Convergence of rational rays in parameter spaces
 by: Carsten Lunde Petersen and Gustav Ryd

- 356/98 Terrænmodellering
Analyse af en matematisk model til konstruktion af digitale terrænmodeller
Modelprojekt af: Thomas Frommelt, Hans Ravnkjær Larsen og Arnold Skimminge
Vejleder: Johnny Ottesen
- 357/98 Cayleys Problem
En historisk analyse af arbejdet med Cayleys problem fra 1870 til 1918
Et matematisk videnskabsfagsprojekt af: Rikke Degn, Bo Jakobsen, Bjarke K. W.
Hansen, Jesper S. Hansen, Jesper Udesen, Peter C. Wulff
Vejleder: Jesper Larsen
- 358/98 Modeling of Feedback Mechanisms which Control the Heart Function in a View to an
Implementation in Cardiovascular Models
Ph.D. Thesis by: Michael Danielsen
- 359/99 Long-Term Scenarios for Global Energy Demand and Supply
Four Global Greenhouse Mitigation Scenarios
by: Bent Sørensen (with contribution from Bernd Kuemmel and Peter Meibom)
- 360/99 SYMMETRI I FYSIK
En Meta-projektrapport af: Martin Niss, Bo Jakobsen & Tune Bjarke Bonné
Vejleder: Peder Voetmann Christiansen
- 361/99 Symplectic Functional Analysis and Spectral Invariants
by: Bernhard Boos-Bavnbek, Kenro Furutani
- 362/99 Er matematik en naturvidenskab? - en udspænding af diskussionen
En videnskabsfagsprojekt-rapport af: Martin Niss
Vejleder: Mogens Nørgaard Olesen
- 363/99 EMERGENCE AND DOWNWARD CAUSATION
by: Donald T. Campbell, Mark H. Bickhard, and Peder V. Christiansen
- 364/99 Illustrationens kraft - Visuel formidling af fysik
Integreret speciale i fysik og kommunikation
af Sebastian Horst
Vejledere: Karin Beyer, Søren Kjørerup
- 365/99 To know - or not to know - mathematics, that is a question of context
by: Tine Wedege
- 366/99 LATEX FOR FORFATTERE - En introduktion til LATEX
og IMFUFA-LATEX
af: Jørgen Larsen

- 367/99 Boundary Reduction of Spectral Invariants and Unique Continuation Property
by: Bernhard Boos-Bavnbek
- 368/99 Kvarvejsrapport for projektet SCENARIER FOR SAMLET UDNYTTELSE AF
BRINT SOM ENERGIBÆRER I DANMARKS FREMTIDIGE ENERGISYSTEM
Projektleder: Bent Sørensen
- 369/99 Dynamics of Complex Quadratic Correspondences
by: Jacob S. Jalving
Supervisor: Carsten Lund Petersen
- 370/99 OPGAVESAMLING - Bredde-Kursus i Fysik 1976 - 1999
Eksamensopgaver fra perioden 1976 - 1999. Denne tekst erstatter
tekst nr. 350/98
- 371/99 Bævisets stilling - beviser og bevisførelse i en gymnasial matematik
undervisning
Et matematikspeciale af: Maria Hermansson
Vejleder: Mogens Niss
- 372/99 En kontekstualiseret matematikhistorisk analyse af ikke-lineær programmering:
Udviklingshistorie og multipel opdagelse
Ph.d.-afhandling af Tinne Hoff Kjeldsen
- 373/99 Criss-Cross Reduction of the Maslov Index and a Proof of the Yoshida-Nicolaescu
Theorem
by: Bernhard Boos-Bavnbek, Kenro Furutani and Nobukazu Otsuki
- 374/99 Det hydrauliske spring - Et eksperimentelt studie af polygoner og hastighedsprofiler
Specialeafhandling af: Anders Marcussen
Vejledere: Tomas Bohr, Clive Ellegaard, Bent C. Jørgensen
- 375/99 Begrundelser for Matematikundervisningen i den lærde skole hhv. gymnasiet 1884-
1914
Historiespeciale af Henrik Andreassen, cand.mag. i Historie og Matematik
- 376/99 Universality of AC conduction in disordered solids
by: Jeppe C. Dyre, Thomas B. Schrøder
- 377/99 The Kuhn-Tucker Theorem in Nonlinear Programming: A Multiple Discovery?
by: Tinne Hoff Kjeldsen

- 378/00 Solar energy preprints:
1. Renewable energy sources and thermal energy storage
2. Integration of photovoltaic cells into the global energy system
by: Bent Sørensen

379/00

EULERS DIFFERENTIALREGNING

Eulers indførelse af differentialregningen stillet over for den moderne
En tredjeseesters projektrapport på den naturvidenskabelige basisuddannelse
af: Uffe Thomas Volmer Jankvist, Rie Rose Møller Pedersen, Maja Bagge Pedersen
Vejleder: Jørgen Larsen

380/00

MATEMATISK MODELLERING AF HJERTEFUNKTIONEN

Isovolumetrisk ventrikulær kontraktion og udpumpning til det cardiovascular system
af: Gitte Andersen (3. moduls-rapport), Jakob Hilmer og Stine Weisbjerg (speciale)
Vejleder: Johnny Ottesen

381/00

Matematikviden og teknologiske kompetencer hos kortuddannede voksne

- Rekognosceringer og konstruktioner i grænselandet mellem matematikkens didaktik
og forskning i voksenuddannelse
Ph. d.-afhandling af Tine Wedege

382/00

Den selvundvigende vandring

Et matematisk professionsprojekt
af: Martin Niss, Arnold Skimminge
Vejledere: Viggo Andreassen, John Villumsen

383/00

Beviser i matematik

af: Anne K.S. Jensen, Gitte M. Jensen, Jesper Thrane, Karen L.A.W. Wille, Peter Wulff
Vejleder: Mogens Niss

384/00

Hopping in Disordered Media: A Model Glass Former and A Hopping Model

Ph.D. thesis by: Thomas B. Schrøder
Supervisor: Jeppe C. Dyre

385/00

The Geometry of Cauchy Data Spaces

This report is dedicated to the memory of Jean Leray (1906-1998)
by: B. Booss-Bavnbek, K. Furutani, K. P. Wojciechowski

386/00

Neutrale mandatfordelingsmetoder - en illusion?

af: Hans Henrik Brok-Kristensen, Knud Dyrberg, Tove Oxager, Jens Sveistrup
Vejleder: Bernhard Booss-Bavnbek

387/00

A History of the Minimax Theorem: von Neumann's Conception of the Minimax Theorem - - a Journey Through Different Mathematical Contexts

by: Tinne Hoff Kjeldsen

388/00

Behandling af impuls ved kilder og dræn i C. S. Peskins 2D-hjertemodel
et 2. moduls matematik modelprojekt

af: Bo Jakobsen, Kristine Niss
Vejleder: Jesper Larsen

389/00

University mathematics based on problemoriented student projects: 25 years of
experience with the Roskilde model

By: Mogens Niss

Do not ask what mathematics can do for modelling. Ask what modelling can do for
mathematics!

by: Johnny Ottesen

390/01

SCENARIER FOR SAMLET UDNYTTELSE AF BRINT SOM ENERGIBÆRER I
DANMARKS FREMTIDIGE ENERGISYSTEM Slutrapport, april 2001

Projektlæder: Bent Sørensen

Projektdeltagere: DONG: Aksel Hauge Petersen, Celia Juhl, Elkraft System¹; Thomas
Engberg Pedersen²; Hans Ravn, Charlotte Søndergren, Energi 2³; Peter Simonsen,
RISØ Systemanalyse⁴; Kaj Jørgensen⁵, Lars Henrik Nielsen, Helge V. Larsen,
Poul Erik Morthorst, Lotte Schleisner, RUC: Finn Sørensen⁶, Bent Sørensen⁷
¹Indtil 1/1-2000 Elkraft, ²fra 1/5-2000 Cowi Consult
³Indtil 15/6-1999 DTU Bygninger & Energi, ⁴fra 1/1-2001 Polypeptide Labs.
Projekt 1763/99-0001 under Energistyrelsens Brintprogram

391/01

Matematisk modelleringskompetence - et undervisningsforløb i gymnasiet

3. semesters Nat.Bas. projekt af: Jess Tolstrup Boye, Morten Bjørn-Mortensen, Sofie
Inari Castella, Jan Lauridsen, Maria Gätzsche, Ditte Mandee Andreassen
Vejleder: Johnny Ottesen

392/01

"PHYSICS REVEALED" THE METHODS AND SUBJECT MATTER OF
PHYSICS

an introduction to pedestrians (but not excluding cyclists)
PART III: PHYSICS IN PHILOSOPHICAL CONTEXT
by: Bent Sørensen.

393/01

Hilberts matematikfilosofi

Specialrapport af: Jesper Hasmark Andersen
Vejleder: Stig Andur Pedersen

394/01

"PHYSICS REVEALED" THE METHODS AND SUBJECT MATTER OF
PHYSICS

an introduction to pedestrians (but not excluding cyclists)
PART II: PHYSICS PROPER
by: Bent Sørensen.

395/01

Menneskers forhold til matematik. Det har sine årsager!

Specialeafhandling af: Anita Stark, Agnete K. Ravnborg
Vejleder: Tine Wedege

396/01

2 bilag til tekst nr. 395: Menneskers forhold til matematik. Det har sine årsager!

Specialeafhandling af: Anita Stark, Agnete K. Ravnborg
Vejleder: Tine Wedege

- 397/01 En undersøgelse af solvents og kædelængdes betydning for anomal swelling i phospholipidbobbeltæg
2. modul fysikrapport af: Kristine Niss, Arnold Skimminge, Esben Thormann, Stine Timmermann
Vejleder: Dorthe Posselt
- 398/01 Kursusmateriale til "Lineære strukturer fra algebra og analyse" (E1)
Af: Mogens Bruun Heefelt
- 399/01 Undergraduate Learning Difficulties and Mathematical Reasoning
Ph.D Thesis by: Johan Lithner
Supervisor: Mogens Niss
- 400/01 On Holomorphic Critical quasi circle maps
By: Carsten Lunde Petersen
- 401/01 Finite Type Arithmetic
Computable Existence Analysed by Modified Realisability and Functional Interpretation
Master's Thesis by: Klaus Provin Jørgensen
Supervisors: Ulrich Kohlenbach, Stig Andur Pedersen and Anders Madsen
- 402/01 Matematisk modellering ved den naturvidenskabelige basisuddannelse
- udvikling af et kursus
Af: Morten Blomhøj, Tomas Højgaard Jensen, Tinne Hoff Kjeldsen og Johnny Ottesen
- 403/01 Generaliseringer i integralteorien
- En undersøgelse af Lebesgue-integralet, Radon-integralet og Perron-integralet
Et 2. modul matematikprojekt udarbejdet af: Stine Timmermann og Eva Uhre
Vejledere: Bernhard Booss-Bavnbek og Tinne Hoff Kjeldsen
- 404/01 "Mere spredt fægning"
Af: Jens Højgaard Jensen
- 405/01 Real life routing
- en strategi for et virkeligt vrp
Et matematisk modelprojekt af: David Heiberg Backchi, Rasmus Brauner Godiksen, Uffe Thomas Volmer Jankvist, Jogvan Martin Poulsen og Neslihan Saglanmak
Vejleder: Jørgen Larsen
- 406/01 Opgavesamling til dybdekursus i fysik
Eksamensopgaver stillet i perioden juni 1976 til juni 2001
Denne tekst erstatter tekst nr. 25/1980 + efterfølgende tillæg
- 407/01 Unbounded Fredholm Operators and Spectral Flow
By: Bernhard Booss-Bavnbek, Matthias Lesch, John Phillips

- 408/02 Weak UCP and Perturbed Monopole Equations
By: Bernhard Booss-Bavnbek, Matilde Marcolli, Bai-Ling Wang
- 409/02 Algebraisk ligningsløsning fra Cardano til Cauchy
- et studie af kombinationers, permutationers samt invariansbegrebets betydning for den algebraiske ligningsløsning for Gauss, Abel og Galois
Videnskabsfagsprojekt af: David Heiberg Backchi, Uffe Thomas Volmer Jankvist, Neslihan Saglanmak
Vejleder: Bernhard Booss-Bavnbek
- 410/02 2 projekter om modellering af influenzaepidemier
Influenzaepidemier- et matematisk modelleringsprojekt
Af: Claus Jørgensen, Christina Lohfert, Martin Mikkelsen, Anne-Louise H. Nielsen
Vejleder: Morten Blomhøj
Influenza A: Den tilbagevendende plage – et modelleringsprojekt
Af: Beth Paludan Carlsen, Christian Dahmeke, Lena Petersen, Michael Wagner
Vejleder: Morten Blomhøj
- 411/02 Polygonformede hydrauliske spring
Et modelleringsprojekt af: Kåre Stokvad Hansen, Ditte Jørgensen, Johan Rønby Pedersen, Bjørn Toldbod
Vejleder: Jesper Larsen
- 412/02 Hopfbifurkation og topologi i væskestrømning – en generel analyse samt en behandling af strømmingen bag en cylinder
Et matematisk modul III professionsprojekt af: Kristine Niss, Bo Jakobsen
Vejledere: Morten Brøns, Johnny Ottesen
- 413/03 "Elevernes stemmer" Fysikfaget, undervisningen og lærerroller, som eleverne opfatter det i det almene gymnasium i Danmark
Af: Carl Angell, Albert Chr. Paulsen
- 414/03 Feltiniediagrammer En vej til forståelse?
Et 1. modul fysikprojekt af: Ditte Gundermann, Kåre Stokvad Hansen, Ulf Rørbæk Pedersen
Vejleder: Tage Emil Christensen
- 415/03 FYSIKFAGET I FORANDRING Læring og undervisning i fysik i gymnasiet med fokus på dialogiske processer, autenticitet og kompetenceudvikling
Ph.d.-afhandling i fysikdidaktik af: Jens Dolin
- 416/03 Fourier og Funktionsbegrebet
- Overgangen fra Eulers til Dirichlets funktionsbegreb
Projektrapport af: Rasmus Brauner Godiksen, Claus Jørgensen, Tony Møyer Hanberg, Bjørn Toldbod
Vejleder: Erik von Essen

417/03

The Semiotic Flora of Elementary particles
By: Peder Voetmann Christiansen

418/03

Militermatematik set med kompetencebriller
3. modul projektrapport af: Gitte Jensen og specialrapport af: Jesper Thrane
Vejleder: Tine Wedege